

# Conditionalisation Revisited

LoPSE seminars

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# Consequences of Conditionalisation

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**Diachronic Conditionalisation:** Let  $\mathcal{B}$  be a set of propositions that includes possible evidence. Let  $c_t$  be your current credence on  $\mathcal{B}$ . Let  $\mathcal{E} = \{E_1, \dots, E_n\}$  be the partition of evidence that you can learn between  $t$  and some later moment  $t + 1$ . Let  $c_{t+1}$  be your credence after learning  $E_i \in \mathcal{E}$ . The conditionalisation rule says that:

$$c_{t+1}(-) = c_t(-|E_i) = \frac{c_t(-\&E_i)}{c_t(E_i)}, \quad (1)$$

where  $c_{t+1}(-)$  is of course defined only for  $c_t(E_i) > 0$ .

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1. When you learn new evidence, one consequence of conditionalisation is that you learn it with certainty.

Proof

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  - 2.3 Stake is determined by the bookie.

# Conditionalisation Retains Certainties

1. Suppose that you assign credence (probability) 1 or 0 to some proposition  $X$  (it can be a proposition which is your evidence  $E_i$ ). Further, suppose you learn new evidence  $E_j$ .

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2. **Different perspective:** Once you rule out some possible worlds by learning, they remain ruled out forever as long as you conditionalise.

# Forgetting Your Evidence

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2. information that is time or agent dependent

- 2.1 I am sure that the proposition that today is Thursday is true. But in 24 hours, I will not be sure any more that the proposition that today is Thursday is true.

## Memory Loss - Talbott's Spaghetti dinner

If we assume that I had spaghetti for dinner one year ago (on March 15, 1989), then where  $t_1$  is 6:30pm on March 15, 1989;  $t_2$  is 6:30pm on March 15, 1990; and  $S$  is the proposition that Talbott had spaghetti for dinner on March 15, 1989. . . if I am assumed to satisfy Temporal Conditionalization at every time from  $t_1$  to  $t_2$ , it must be the case that I be as certain of  $S$  at  $t_2$  as I was at  $t_1$  . . . But, in fact (and I knew this at  $t_1$ ), if at  $t_2$  I am asked how probable it is that I had spaghetti for dinner on March 15, 1989, the best I can do is to calculate a probability based on the relative frequency of spaghetti dinners in my diet one year ago.

Talbott, W.J. Two Principles of Bayesian Epistemology, *Philosophical Studies*, 62, 1991, p. 135–150.

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3. But there is another example show that we need more than just an assumption that ideally rational agents do not forget.

## Memory Loss - Two Paths to Shangri La

There are two paths to Shangri La, the Path by the Mountains, and the Path by the Sea. A fair coin will be tossed by the guardians to determine which path you will take: if heads you go by the Mountains, if tails you go by the Sea. If you go by the Mountains, nothing strange will happen: while traveling you will see the glorious Mountains, and even after you enter Shangri La, you will forever maintain your memories of that Magnificent Journey. If you go by the Sea, you will revel in the Beauty of the Misty Ocean. But, just as you enter Shangri La, your memory of this Beauteous Journey will be erased and be replaced by a memory of the Journey by the Mountains.

Arntzenius, F. Some Problems for Conditionalization and Reflection, *The Journal of Philosophy*, 100(7), 2003, p. 356–370.

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- 1.4 You know you would possess those memories whichever path you travelled, so you take them as no evidence about the outcome of the coin and, presumably, assign credence  $1/2$  to  $H$

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  - 2.1 You violate conditionalisation only when you merely suspect you may have forgotten something.
  - 2.2 It might be irrational to forget something.
  - 2.3 But is it irrational to assign credence bigger than 0 to the contingent possibility that one forgot something at some point in the past?

# Slippery Evidence

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7. Possible worlds, as we have discussed them so far, are too coarse-grained descriptions to give us answer.
8. We need to introduce more fine-grained entities than classical possible worlds.

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4. **Centred propositions** such as 'it is 1pm now' can be represented as sets of centred possible worlds.
5. We can call classical possible worlds **uncentred worlds** and propositions represented by sets of uncentred possible worlds as **uncentred propositions**.

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5. Conditionalisation presupposes that an agent's evidence may change, but the truth-values of the target propositions remain fixed.
6. Yet centred propositions present the agent with moving targets; as she gains (or loses) information, their truth-values may change as well.

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    - 1.3.1 Take a particular uncentered world (call it  $u$ ). Consider all the centres associated with that world you entertained as live possibilities at  $t_j$ . Assign credence 0 to any centred world incompatible with  $E$ . Then take the credence assigned to  $u$  in Step 1 above, and distribute it among the remaining centred worlds associated with that uncentered world.

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2. **Notice:** The second step is underspecified. It does not say how we should distribute credences among the centred worlds.

## How Do We Update on Centred Propositions?

Example - Titlebaum p. 380

At  $t_1$ , you have no idea what time it is. You are wearing a watch that you are 60% confident is running reliably. The rest of your credence is divided equally between the possibility that the watch is entirely stopped, and the possibility that it is running but is off by an exactly an hour (perhaps due to daylight savings). You then glance at your watch, notice that it is running (the second hand is moving), and that it currently reads 1pm.

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Example Continued - Titlebaum p. 380

stopped	initial c	running and shows 1pm – step 1
stopped	0.2	0
reliable	0.6	0.75
1 hour off	0.2	0.25

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Example Continued - Titlebaum p. 380

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Take for example  $w_1$ :  $(w_1, 12pm)$ ,  $(w_1, 1pm)$ ,  $(w_1, 2pm)$ .

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  - 2.1  $c(w_1, 12pm) = 0$ ,  $c(w_1, 1pm) = 0$ ,  $c(w_1, 2pm) = 0$ .

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Take for example  $w_1$ :  $(w_1, 12pm)$ ,  $(w_1, 1pm)$ ,  $(w_1, 2pm)$ .
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# How Do We Update on Centred Propositions?

Example Continued - Titlebaum p. 380

stopped	step 1
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reliable	0.75
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  - 3.2 We can, for example, use foundationalist epistemologies – e.g. sense data and phenomenal experiences are certain.

# Jeffrey Conditionalisation

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# Motivation

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2. If an agent updates by Conditionalization and gains no certainties between two times, it must be because she gained no evidence between those times.
3. But we seem to gain evidence between two times that is not certain (or should not be certain if you agree with the Regularity Principle).

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3. But we seem to gain evidence between two times that is not certain (or should not be certain if you agree with the Regularity Principle).
4. What do we do then?

## Jeffrey Conditionalisation

**Jeffrey Conditionalisation** Given any  $t_i$  and  $t_j$  with  $i < j$ , any  $X$  in  $\mathcal{L}$ , and a finite partition  $B_1, B_2, \dots, B_n$  in  $\mathcal{L}$  whose elements each have non-zero  $cr_i$ ,

$$cr_j(X) = cr_i(X|B_1) \times cr_j(B_1) + \dots + cr_i(X|B_n) \times cr_j(B_n) \quad (2)$$

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**Notice:** Jeffrey Conditionalisation reduces to classical conditionalisation when I learn evidence with certainty from a partition.

Suppose that you learn  $B_1$  with certainty from the finite partition  $B_1, B_2, \dots, B_n$ .

$$\begin{aligned} cr_j(X) &= cr_i(X|B_1) \times 1 + \dots + cr_i(X|B_n) \times 0 \\ &= cr_i(X|B_1) \end{aligned} \quad (3)$$

## Classical Example

### Example

The agent inspects a piece of cloth by candlelight, and gets the impression that it is green, although he concedes that it might be blue or even (but very improbably) violet. If  $G$ ,  $B$ , and  $V$  are the propositions that the cloth is green, blue, and violet, respectively, then the outcome of the observation might be that, whereas originally his degrees of belief in  $G$ ,  $B$ , and  $V$  were 0.3, 0.3, and 0.4, his degrees of belief in those same propositions after the observation are 0.7, 0.25, and 0.5.

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The worry is that even if we grant the existence of a sense datum for each potential learning experience, the quality of that sense datum might not be representable in a proposition to which the agent could assign certainty

## Concrete Example – Titlebaum p. 160

### Example Continued

Suppose that:

$$c_1(G) = 0.3 \quad c_1(B) = 0.3 \quad c_1(V) = 0.4$$

and

$$c_1(\text{mine}|G) = 0.8 \quad c_1(\text{mine}|B) = 0.5 \quad c_1(\text{mine}|V) = 0$$

and

$$c_2(G) = 0.7 \quad c_2(B) = 0.25 \quad c_2(V) = 0.05$$

so by Jeffrey conditionalisation

$$\begin{aligned} c_2(\text{mine}) &= c_1(\text{mine}|G)c_2(G) + c_1(\text{mine}|B)c_2(B) + c_1(\text{mine}|V)c_2(V) \\ &= 0.80 * 0.70 + 0.50 * 0.25 + 0 * 0.05 \\ &= 0.685 \end{aligned}$$

(4)

### Example Continued

$$c_2(\text{mine}) = c_1(\text{mine}|G)c_2(G) + c_1(\text{mine}|B)c_2(B) + c_1(A|V)c_2(V) \quad (5)$$

Use the Law of Total probability on  $c_2(\text{mine})$

$$c_2(\text{mine}) = c_2(\text{mine}|G)c_2(G) + c_2(\text{mine}|B)c_2(B) + c_2(A|V)c_2(V) \quad (6)$$

It must be the case that

$$c_1(\text{mine}|G) = c_2(\text{mine}|G), c_1(\text{mine}|B) = c_2(\text{mine}|B) \dots \quad (7)$$

**Rigidity:** For any  $A$  in  $\mathcal{L}$  and any  $B_m$  in  $B_1, B_2, \dots, B_n$

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Jeffrey Conditionalisation using a particular partition  $B_1, B_2, \dots, B_n$  is appropriate only when the agent's credences conditional on the  $B_m$  remain constant across two times.

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2. Jeffrey Conditionalisation is **not commutative**. It matters in which order we learn evidence (classical conditionalisation is commutative).

## Caveat: Bayes' Theorem

1. Remember conditional credences? Suppose that we have some hypothesis  $H$  and evidence  $E$ , the  $c(H|E)$  is the probabilistic credence that  $H$  is true given that we suppose that  $E$  is true.

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$$\text{Bayes' Theorem: } c(H|E) = \frac{c(E|H)*c(H)}{c(E)} \text{ for } c(E) \neq 0.$$

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# Non-Commutativity of Jeffrey Conditionalisation

## Raven Example

Suppose I see a bird at twilight, and I clearly identify it to be a raven. Because of the difficulty in identifying the bird's color in the gloom, I do not observe that  $e$  – “The bird is black” – but the effect of my experience is to raise my confidence in  $e$  from 0.75 to 0.99. If  $h$  is “All ravens are black” and my background beliefs include that the bird is a raven.

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## Raven Example - Reversed Order of Evidence

Suppose I see a bird at twilight, and I clearly identify it to be a raven. Because of the difficulty in identifying the bird's color in the gloom, I do not observe that  $e$  – “The bird is black” – but the effect of my experience is to raise my confidence in  $e$  from 0.75 to **0.8**. If  $h$  is “All ravens are black” and my background beliefs include that the bird is a raven.

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1. Suppose that I take a second glance on a bird. I am more confident now, and so my credence in  $e$  is now 0.99. So my  $c_{new}(e) = 0.99$ ,  $c_{old}(e) = 0.8$ ,  $c_{old}(\neg e) = 0.2$ , and  $c_{old}(h) \approx 0.747$ .

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- 1.5  $c_{new}(h) = 0.933 * 0.99 + 0 * 0.01 \approx 0.924$

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2. **Notice:** In this example, the result of successive applications of Jeffrey conditionalization firstly to  $c(e) = 0.99$  and then  $c(e) = 0.8$  is indeed the same as the result of applying Jeffrey conditionalization once first to  $c(e) = 0.8$ , as if the 0.99 experience had never occurred (this does not happen always).

# Slippery Evidence – Problem for Jeffrey Conditionalisation

## Raven Example – modified Titlebaum p. 378

- 0.1 I look out of a window. I see drops of water on my window. Experience directly influences my credences over the partition containing the centred propositions 1.) it's raining now and 2.) it's not raining now (maybe my neighbour is just watering his flowers.) I want to set my unconditional credence in the proposition  $S$  that it rains on (a specific) Sunday.

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- 0.2 Suppose that  $e(\neg e)$  stands for 'it's (not) raining now'. By Jeffrey conditionalisation:

$$c_{new}(S) = c_{old}(S|e) * c_{new}(e) + c_{old}(S|\neg e) * c_{new}(\neg e) \quad (9)$$

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0.3 Whatever  $c_{new}(e)$  and  $c_{new}(\neg e)$  are, by the Bayes' Theorem:

$$c_{old}(S|e) = \frac{c_{old}(e|S) * c_{old}(S)}{c_{old}(e)} \quad (10)$$

The value of  $c_{old}(S|e)$  has to remain the same (by rigidity).

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- 1.1 Suppose 'now' means Sunday. Further, suppose that my initial credence in  $S$  (before the experience) is 0.5, the experience raised my credence in  $e$  from 0.6 to 0.8, and  $1 > c_{old}(e|S) > 0$ , then:

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so  $1 > c_{old}(S|e) > 0$ .

- 1.2 Suppose 'now' means Monday. On Monday you know whether it rained on that specific Sunday, so  $c_{old}(S|e) = 1$  if it rained and  $c_{old}(S|e) = 0$  if it did not rain.

Thank you!