

# Introduction to Theories of Confirmation

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# Deductive Reasoning

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Example: Modus Ponens

**Premise 1:** If I am blushing, I feel guilty.

**Premise 2:** I am blushing.

**Conclusion:** I feel guilty.

$B$ (premise 2)	$G$ (conclusion)	$B \rightarrow G$ (premise 1)
<b>T</b>	<b>T</b>	<b>T</b>
T	F	F
F	T	T
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**Conclusion:** All swans are white.

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2. When we talk about some concepts such as credences, comparative beliefs, etc. we want to postulate some desirable properties that such concepts should meet.
3. The same idea applies to confirmation. We want to know what properties confirmation should and can have without running to paradoxical conclusions.
4. To find such properties has proved to be difficult. Let us take a look at some examples.

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## Paradox of Ravens

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2. Two condition he accepted are Nicod's Criterion and Equivalence Condition, but they proved to be difficult to combine.
3. Their combination leads to the Paradox of Ravens.

## Nicod's Criterion

**Nicod's Criterion:** For any predicates  $F$  and  $G$  and constant  $a$  of  $\mathcal{L}$ ,  $(\forall x)(Fx \rightarrow Gx)$  is confirmed by  $Fa$  &  $Ga$  and disconfirmed by  $Fa$  &  $\neg Ga$ .

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Example: White Swans

Think of the predicate  $S$  as being a swan and  $W$  as being white. Suppose that the constant  $a$  stands for a particular swan.

Nicod's criterion then says that the hypothesis that "all swans are white" e.i.  $(\forall x)(Sx \rightarrow Wx)$  is confirmed by an instance of a white swan e.i.  $Sa \ \& \ Wa$  and disconfirmed by an instance of a black swan e.i.  $Sa \ \& \ \neg Wa$ .

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**Equivalence Relation:** Suppose  $H$  and  $H'$  in  $\mathcal{L}$  are logically equivalent ( $H \equiv H'$ ). Then any  $E$  in  $\mathcal{L}$  that confirms  $H$  also confirms  $H'$ .

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2. When evidence  $E$  confirms a hypothesis  $H$  and  $H$  is equivalent to  $H'$ , then  $E$  confirms also  $H'$ .

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4. By the Nicod's Criterion  $\neg Ba \ \& \ \neg Ra$  confirms  $(\forall x)(\neg Bx \rightarrow \neg Rx)$ .
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6. By Equivalence Relation  $\neg Ba \ \& \ \neg Ra$  confirms  $(\forall x)(Rx \rightarrow Bx)$ .

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4. This result is counterintuitive.

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  - 1.5 But our  $k$  should contain no contingent propositions. Against that background knowledge, confirmation works, says Hempel.
  - 1.6 Suppose that we randomly pick things from the universe one by one and we know that picking a non-black raven falsifies our hypothesis that all ravens are black. Picking a thing that is a non-black raven somewhat confirms our hypothesis that all ravens are black.

# Evidence of Evidence

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## What Are Other Confirmation Conditions

**Entailment Condition:** For any consistent  $E$ ,  $H$ , and  $K$  in  $\mathcal{L}$ , if  $E \& K \Rightarrow H$  but  $K \not\Rightarrow H$ , then  $E$  confirms  $H$  relative to  $K$ .

1. Entailing a hypothesis  $H$  is a method of supporting or providing evidence for that hypothesis (given some background knowledge  $K$ ).
2. It works only if  $K$  itself does not imply  $H$

## What Are Other Confirmation Conditions

**Confirmation Transitivity:** For any  $A, B, C$  and  $K$  in  $\mathcal{L}$ , if  $A$  confirms  $B$  relative to  $K$  and  $B$  confirms  $C$  relative to  $K$ , then  $A$  confirms  $C$  relative to  $K$ .

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- 2.) A: This is a white swan in the house of curiosities.
- 3.) B: This is a white swan.
- 4.) C: All swans are white.
- 5.) A entails B and by Entailment, A confirms B. But B also confirms C. If we take confirmation to be transitive, then A should confirm C. But it sounds strange. If a white swan is a curiosity, it rather disconfirms that all swans are white.

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2. Imagine I read a police transcript of interrogation. In the transcript, the interrogate admits committing the crime (I do not have the actual evidence – I did not hear him saying that). Does the transcript constitute an evidence against the perpetrator?

## Triviality Result

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1. **Problem:** Any relation of confirmation satisfying 1, 2, and 4 is trivial in the sense that every evidential proposition  $E$  confirms every hypothesis  $H$ .

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5. Hempel rejects the converse consequence condition as the culprit rendering the triviality result.

# HD-Confirmation and Underdetermination

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**hypothesis** Light exhibits wavelike behaviour.

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**evidence** An interference pattern is displayed on the screen.

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- iii  $e$  is HD-neutral for hypothesis  $h$  relative to  $k$  otherwise.;

## Example 1

Our best theories about the atmospheric system suggest that emissions of greenhouse gases such as  $CO_2$  and Methane lead to global warming. That hypothesis has been vindicated by its successful (qualitative) predictions, such as shrinking arctic ice sheets, increasing global temperatures, its ability to backtrack temperature variations in the past, etc.

# HD-Confirmation Examples

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## Example 2

Einstein's General Theory of Relativity predicted that light would be bent by massive bodies like the sun. The vindication of Einstein's forecasts by Eddington during the 1919 eclipse contributed a lot to the general acceptance of GTR.

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1. HD-confirmation can accommodate the Paradox by using the auxiliary assumptions.
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- 0.4 The observation of a black swan turns out to be HD-neutral for the hypothesis that black swans exist

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- 0.4 While HD-neutral for  $h$ ,  $e$  HD-disconfirms  $\neg h$ , and thus does not meet confirmation complementarity.

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6. This is simply because, if  $h \wedge k \Rightarrow e$ , then  $h \wedge k \wedge q \Rightarrow e$ , too, by the monotonicity of classical logical entailment.

# Popper's Falsificationism

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  - 3.1 We only need to find a piece of metal that does not conduct electricity in order to know that our hypothesis is fals.
4. Popper suggested that all science should put forth bold hypotheses, which are then severely tested (where 'bold' means to have many observational consequences). As long as these hypotheses survive their tests, scientists should stick to them. However, once they are falsified, they should be put aside if there are competing hypotheses that remain unfalsified.

Thank you!